

T1 P is the midpoint of AB.

$$\therefore AP = BP$$

$$\angle EPA + \angle EPD = \angle BPB + \angle EPD$$

$$\Rightarrow \angle APD = \angle BPE.$$

(i) Now, in $\triangle DAP$ and $\triangle EBP$ we have

$$\angle PAD = \angle PBE \quad (\because \angle BAD = \angle ABE).$$

$$AP = BP \quad (\text{Proved above})$$

$$\angle DPA = \angle EPB \quad [\text{proved above}].$$

$$\triangle DAP \cong \triangle EBP \quad [\text{By ASA congruency}].$$

(ii) since, $\triangle DAP \cong \triangle EBP$

$$\Rightarrow AD = BE \quad [\text{By CPCT}].$$

T2 In $\triangle ABD$ and $\triangle ACD$, we have

(i) $AB = AC$ [Given].

$$AD = DA \quad [\text{Common}]$$

$$BD = CD \quad [\text{Given}].$$

$$\therefore \triangle ABD \cong \triangle ACD \quad [\text{By SSS congruency}].$$

$$\angle BAD = \angle CAD \quad [\text{By C.P.C.T.}], \rightarrow \textcircled{1}$$

(ii) In $\triangle ABP$ and $\triangle ACP$, we have

$$AB = AC \quad [\text{Given}].$$

$$\angle BAP = \angle CAP \quad [\text{From } \textcircled{1}]$$

$$\therefore AP = PA \quad [\text{common}].$$

$$\therefore \triangle ABP \cong \triangle ACP \quad [\text{By SAS congruency}].$$

(iii) since $\triangle ABP \cong \triangle ACP$

$$\Rightarrow \angle BAP = \angle CAP \quad [\text{By CPCT}].$$

$\therefore AP$ is the bisector of $\angle A$.

in $\triangle BDP$ and $\triangle CDP$

$$\text{we have } BD = CD \quad [\text{Given}]$$

$$DP = PD \text{ [common]}$$

$$BP = CP [\because \triangle ABP \cong \triangle ACP].$$

$$\Rightarrow \angle BDP = \angle CDP \text{ [By SSS congruency]}.$$

DP is the bisector of $\angle BDC$

$\therefore AP$ is the bisector of $\angle A$ and $\angle D$.

$$(iv) \text{ As } \triangle ABP \cong \triangle ACP$$

$$\Rightarrow \angle APB = \angle APC, BP = CP \text{ [By C.P.C.T.]}$$

$$\text{But } \angle APB + \angle APC = 180^\circ \text{ [Linear Pair]}.$$

$$\therefore \angle APB = \angle APC = 90^\circ$$

$$\Rightarrow AP \perp BC \text{ \& also } BP = CP.$$

Q5 Given

$$5x + 3y = 190 \rightarrow (1)$$

$$3x + 2y = 118 \rightarrow (2)$$